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## Wind, solar and battery micro-grid optimal sizing in Tilos Island

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### Abstract

This paper presents a flexible power plant modeling associated with a Multi-Objective Particle Swarm Optimization in order to obtain the optimal size of each plant component. The modeling can be adapted to a wide range of energy sources, storages and loads. The methodology is applied to a Wind Turbine / Photovoltaic array / Battery bank configuration located in Tilos, Greece. The optimization is set up to minimize the system cost and the energy imported from non-renewable sources. The results form a Pareto front representing the trade-off between the equipment cost and the micro-grid autonomy. An optimal solution for a given energy importation cost is detailed as an example.

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*Keywords:* Hybrid power-plant; Particle swarm optimization; Techno-economic study

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### 1. Introduction

Energy production and distribution in non-interconnected areas are often costly and not environmental friendly. This is especially true for islands [1] where the plants heavily rely on fossil fuel or on undersea cables, causing important power losses. Local energy production from renewable sources can help to reduce the energy cost and its environmental impact. To supply power to the consumers at all times, renewable energy power plants should include an energy storage system due to the intermittent nature of the sources [2]. Coupling wind and solar power can also help reduce the production variability [3].

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Such a power plant is expensive and can easily be not profitable if improperly sized [4], [5]. This problem has often been studied in the literature [6] with different algorithms such as Genetic Algorithm [7], [8] or Particle Swarm Algorithm [9], [10]. However each of these references focuses on a specific power plant configuration.

The methodology presented in this paper uses a 12-variable modeling applicable to a wide range of micro-grid configurations [11]. It uses a Multi Objective Particle Swarm Optimization (MOPSO) algorithm [12], [13] to minimize the system cost [14] and the dependence to external energy sources. This external energy cost is used after the optimization to obtain the best plant configuration for a given location and consumption profile.

The algorithm is used to size a wind and solar power plant associated with a battery bank in Tilos Island, Greece. The next section describes the flexible plant modeling, how it is configured for the case studied, its power sources, the energy conversion components, the energy management strategy and the economic assumptions. Section 3 briefly presents the optimization problem and the MOPSO algorithm. Finally, the optimization results are presented in Section 4.

## 2. Plant Modeling

### 2.1. Flexible plant modeling

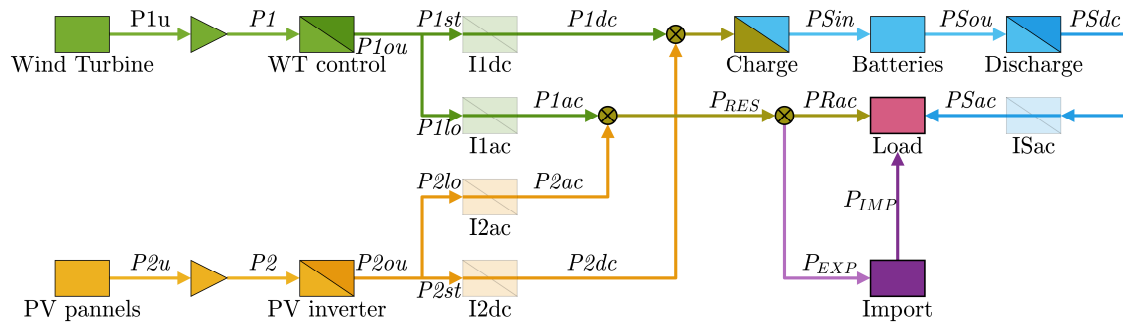
The modeling used in this paper is designed to be modular. It can simulate a wide range of plant configurations made of one or two Renewable Energy Systems (RES) and one External Storage System (ESS). The plants modeled have to supply a load either at all times or with a Loss of Power Supply tolerance. They can be connected to a main grid or a controllable source like a Diesel Generator if the RES power is not sufficient and may or may not export the exceeding energy produced. This flexibility is offered by nine Generic Conversion Systems (GCS) that can be enabled or disabled depending on the configuration modeled.

Fig. 1 presents the algorithm setup for the plant used as an example in this paper. It is made of a Wind Turbine, a Photovoltaic array and a Sodium Nickel Chloride battery bank. The plant is located in Tilos, Greece, and has to supply power to approximately 800 inhabitants [15]. In case the RES are not sufficient to power the load, energy can be produced by a Diesel Generator or imported via an undersea cable from Kos, a nearby island.

### 2.2. Renewable Energy Systems

The Wind Turbine and the PV panels power output is computed from meteorological weather data measured in-situ. The computations are done before the optimization with a unitary installed power then the output is multiplied by the actual installed power. In addition to these RES, the plant can use an undersea cable or a Diesel Generator to import power.

Fig. 1. Algorithm setup for the plant configuration.



To prevent the algorithm from returning a costly solution with almost no energy imported, an economic criterion need to be also minimized.

### 2.5. Economics

Estimating the cost of a power plant is a difficult task due to the number of economic parameters at stake and their variability. The cost for installed PV panel for example decreased by 83% in seven years [17]. They also depend on the supplier, the location and the labor cost and are subject to change quickly. The values used come from [17] and [18] for PV panels and inverters, from [19] for Wind Turbines and from [18] and [20] for the batteries. The authors insist that this paper focuses on the modeling and the optimization methods and that the costs used are purely indicative.

Each component has an installation cost  $C_I$  that depends on its size. The number of replacement  $N_R$  is derived from the equipment lifespan  $L_s$  and the study duration  $D_S$  set here as 25 years. The buying cost is then the  $N_R$  times the installation cost adjusted by the actualization rate  $\tau_A$  that represents the yearly cost variation. The buying cost is divided by the study duration to obtain an annualized cost:

$$C_{BA} = \sum_{k=0}^{N_R} \frac{C_I(1-\tau_A)^{L_s}}{D_S} \quad (1)$$

The annual maintenance cost is assumed to be a fraction  $\tau_M$  of the installation cost. The annualized cost for a given equipment is finally:

$$C_A = C_{BA} + C_I \tau_M \quad (2)$$

The Annualized Cost of System (ACS) is then obtained by summing the annualized cost of each equipment. The ACS is used as the second objective to minimize in the optimization. Since it conflicts with the energy imported, the optimization results will form a Pareto front.

### 3. Particle Swarm Optimization

The optimization problem aims to minimize the Annualized Cost of System (ACS) and the imported energy  $E_{IA}$  under the constraints that the Lost of Power Supply Probability ( $LPSP$ ) is null. It can be formulated as follows:

$$\text{Find } x^* \text{ in } X \text{ such as } \begin{cases} x^* = \arg \min_{x \in X} [ACS(x), E_{IA}(x)] \\ LPSP(x^*) = 0 \end{cases} \quad (3)$$

Where  $x$  is the vector defining the Wind Turbine nominal power, the PV array peak power, the PV inverter rated power and the battery bank capacity and  $X$  the study domain.

This four-parameter optimization problem is solved using a Multi-Objective Particle Swarm Optimization (MOPSO) [13], [21]. It is a gradient-free stochastic algorithm that can solve large scale problems. It works by moving the particles  $x$ , representing plant configurations, in the study domain. The particle speed is derived from the plant performances:  $ACS$  and  $E_{IA}$  so they converge to the optimal solution, if any. The algorithm returns a list of non-dominated plants forming a Pareto front.

### 4. Optimization results

The solutions given by the algorithm are represented by the dark blue line in Fig. 2. Each point in the graph represents an optimal plant with its ACS and the imported energy percentage:  $E_{IA}/E_{CA}$ . The blue circle denotes the actual configuration installed and the thinner lines represent the Wind Turbine nominal power (green), the PV array peak power (yellow) and the battery bank capacity (light blue).

These results indicate that the principal energy source should be the wind. Above 25% imported energy, the plant solely relies on the wind and on the importations without solar power or storage. Below this threshold, increasing the PV array size becomes profitable. However, since this power is not available at night, it should be associated with a bigger storage. This increases drastically the cost and gaining in autonomy becomes expensive.

The optimal solution depends now on the cost of producing energy with the Diesel Generator and on the energy importation cost. These costs may vary every hour and should be treated separately. For the sake of illustration, they are supposed equal and constant so the results can be plotted in a 3D graph.

Let  $C_B$  be the energy buying cost (i.e. the importation and the diesel cost). For each plant, the production cost  $C_p$  can be defined as the ratio between the money spent in one year and the energy consumed:

$$C_p = \frac{ACS + C_B E_{IA}}{E_{CA}} \quad (4)$$

For a given  $C_B$ , the plant in the Pareto front that minimizes  $C_p$  is plotted in red in Fig. 3. In the end, assuming  $C_B$  allows to find the optimal component size of the plant, defines the ACS, the imported energy and the production cost. Fig. 4 synthetizes these results on the same figure. For example, for  $C_B = 220$  €/MW.h, the optimal plant is made of a 1 MW Wind Turbine, a 200 kWp PV array with associated with inverters accounting for 350kW nominal power and a 400 kW.h power bank. This plant offers 80% energetic autonomy and a production cost of 87 €/MW.h. This configuration is marked by a red circle in Fig. 2. It uses more wind power and less storage than its actual counterpart for slightly better performances.

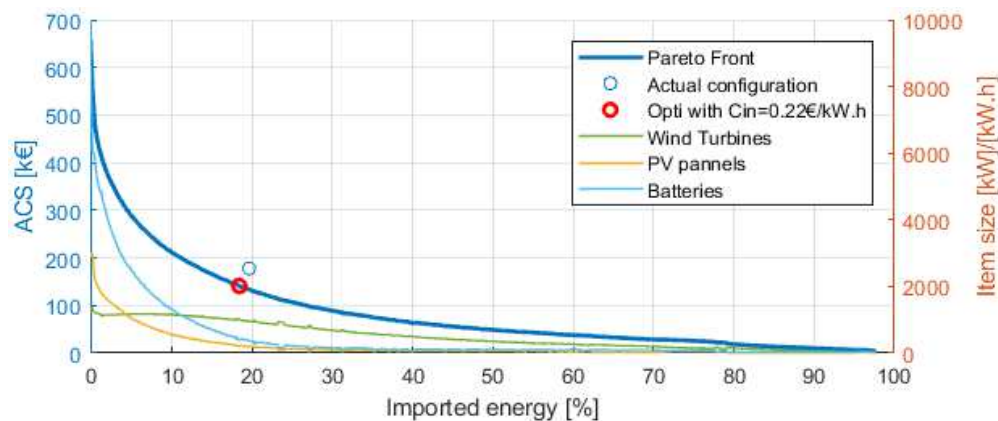


Fig. 2. Algorithm optimization result for a Wind Turbine / Photovoltaic array / Battery bank configuration in Tilos.

## 5. Conclusion

The algorithm presented in this paper is able to optimize the component sizes of a hybrid renewable power plant associated with a storage. The plant model can be adapted to various configurations and takes into account the non-linear cost of the equipment and power dependent efficiencies. A Multi Objective Particle Swarm algorithm is used to solve the optimization problem.

The algorithm has been applied to a Wind Turbine / Photovoltaic array / Battery bank power plant in Tilos Island, Greece. To avoid assuming an energy importation cost before the optimization, the objectives are to minimize the Annualized Cost of System and the imported energy. Once the Pareto front is obtained, the optimal solution for different importation costs can be computed. The solution consists on the size of each plant component (WT size, PV installed power, inverter nominal power and storage capacity), the ACS, the imported energy and the energy production cost.

This algorithm has successfully solved the optimization problem. It can be improved by implementing a better energy management strategy [22], the possibility to use multiple storages, more precise power sources models or the eventual storage aging. Furthermore, the economic parameters for the components buying and maintenance costs need to be refined to give more realistic solutions.

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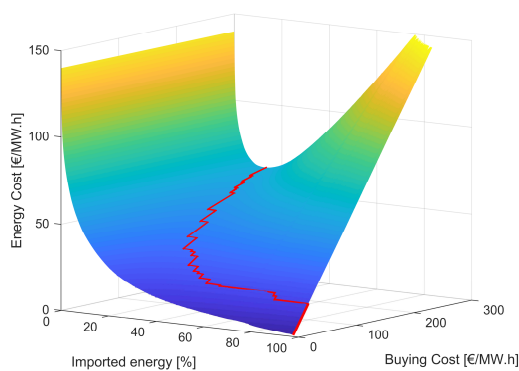


Fig. 3. Energy production cost depending on the optimal solution and the buying cost. The red line denotes the minimal production cost for each buying cost.

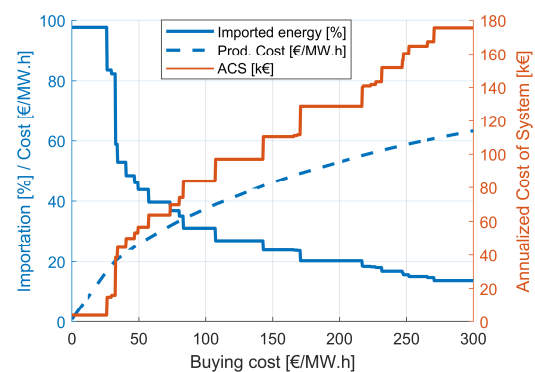


Fig. 4. Annualized Cost of System, Imported Energy and Production Cost versus the Buying Cost.

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